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# Modeling and simulation of non-isothermal catalytic packed bed membrane reactor for H<sub>2</sub>S decomposition

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#### Abstract

The recovery of  $H_2$  from  $H_2S$  is an economical alternative to the Claus process in petroleum and minerals processing industries. Previous studies [React. Kinet. Catal. Lett. 62 (1997) 55; Catal. Lett. 37 (1996) 167] have demonstrated that catalytic decomposition of  $H_2S$  over bimetallic sulfide can proceed at relatively higher rates than over mono-metallic systems due to chemical synergism although conversions are still thermodynamically limited. In the present study, the performance of a catalytic membrane reactor containing a packed bed of Ru–Mo sulfide catalyst has been investigated with a view to improving  $H_2$  yield beyond the equilibrium ceiling. A system of differential equations describing the non-isothermal reactor model has been solved to examine the effect of important hydrodynamic and transport properties on conversion. The results were obtained using a Pt-coated Nb membrane tube as the catalytic reactor enclosed in a quartz shell cylinder. Reynolds number for shell and tube side ( $Re^s$  and  $Re^t$ ) as well as the modified wall Peclet number,  $Pe_m$ , dramatically affect  $H_2S$  conversions. Membrane reactor conversion rose monotonically with axial distance exceeding the equilibrium conversion by as much as eight times under some conditions. © 2000 Elsevier Science B.V. All rights reserved.

Keywords: Claus process; Catalytic packed bed membrane reactor; H2S decomposition

## 1. Introduction

Large quantities of H<sub>2</sub>S produced during petroleum hydrotreatment operations and metal ore reduction processes are often removed from industrial gaseous effluent via the Claus reaction or absorption into alkanolamines. Although re-salable sulfur may be obtained, these H<sub>2</sub>S removal options convert useful H<sub>2</sub> into non-profitable low grade water. The catalytic decomposition of H<sub>2</sub>S to hydrogen and sulfur, both of which are highly valuable, offer the possibility for improving overall plant economics [3].

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Several investigators have examined the catalytic splitting of  $H_2S$  over transition metal sulfides. Evidence suggests that bimetallic Mo-containing sulfides exhibit some of the best activities [1,2]. However, since the reaction is reversible and strongly endothermic ( $\Delta H_{298} = 85.2 \, \text{kJ/mol}$ ), conversion and  $H_2$  yield are limited by thermodynamics. It is therefore expected that a system in which simultaneous product  $H_2$  separation from the reaction can take place will improve process performance. A catalytic packed bed membrane reactor immediately suggests itself.

Buxbaum and Kinney [4] have presented H<sub>2</sub> permeation data for several metals as a function of temperature. Since catalytic H<sub>2</sub>S decomposition proceeds only at reasonable rates from about 873 K, the reactor would be fabricated from metallic membranes that

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#### Nomenclature

A reactor cross-sectional area

 $C_p$  heat capacity of gas

d thickness of membrane

F volumetric flow rate

h overall heat transfer coefficient

 $\Delta H$  heat of the H<sub>2</sub>S decomposition reaction

J flux across the membrane

*k* reaction rate constant

 $K_{\rm eq}$  equilibrium constant for  $H_2S$ 

decomposition reaction

L reactor length

M molecular weight

P partial pressure

P permeability

Pem modified Peclet number

 $r_{\rm H_2S}$  rate of reaction Re Reynolds number

S surface area per unit length

T temperature

z dimensionless reactor length coordinate

#### Greek letter

 $\mu$  viscosity of gas

#### Subscript

Ar argon gas

H<sub>2</sub> hydrogen gas

H<sub>2</sub>S hydrogen sulfide gas

M membrane

mix gas mixture

tot total

i component i

### Superscripts

f furnace

in inlet

s shell side

t tube side

show excellent permeation coefficient and  $H_2$  permselectivity at this elevated temperature. Among others, niobium offers an excellent  $H_2$  permeation rate in the range 700–1100 K. To avoid  $H_2S$  corrosion at these temperatures, Nb tube would be internally coated with platinum which also enjoys comparable  $H_2$  permeability. Thus the packed bed reactor consisted of a composite Nb/Pt membrane encased in a quartz cylinder (shell). The annular space between the Nb/Pt tube and the quartz shell is swept by an inert gas to carry away the permeated  $H_2$ . The membrane tube is packed with a Ru–Mo sulfide since the kinetic expression for  $H_2S$  decomposition over this catalyst has been previously obtained [2].

In view of the endothermic nature of the reaction, the catalytic packed bed membrane reactor (CPBMR) is deemed to operate non-isothermally. The present work is therefore focused on a parametric study of the reactor system to provide a basis for experimental optimization.

# 2. Model development

A schematic diagram of the shell-and-tube membrane reactor is shown in Fig. 1. The sweep gas through the shell (annulus) side is pure (inert) argon while the feed is an H<sub>2</sub>S/argon mixture. Both streams are preheated to at least 873 K before entering the reactor system which is itself placed in a temperature-controlled furnace. For the purpose of model development, it is assumed that:

- 1. plug flow conditions exist in both shell and tube sides;
- 2. negligible axial pressure drop prevails in both packed bed and annular space;
- 3. constant sweep gas flow rate since permeated H<sub>2</sub> flow rate is relatively low;
- 4. H<sub>2</sub> permeation through the Nb/Pt membrane follows Sievert's law [5], thus, cross-flow H<sub>2</sub> flux,  $J_{\text{H}_2}$ , is

$$J_{\rm H_2} = U[(P_{\rm H_2}^{\rm t})^{1/2} - (P_{\rm H_2}^{\rm s})^{1/2}] \tag{1}$$

where the overall permeation coefficient, *U*, is related to H<sub>2</sub> permeability through Pt and Nb as

$$\frac{1}{U} = \frac{d_{\text{Pt}}^{\text{m}}}{\mathcal{P}_{\text{Pt}}} + \frac{d_{\text{Nb}}^{\text{m}}}{\mathcal{P}_{\text{Nb}}}$$
 (2)

Neither  $H_2S$  nor  $S_2$  molecules permeate through to the shell side, i.e. 100%  $H_2$  permselectivity;

- 5. membrane is catalytically inactive;
- 6. reactant and sweep gas flow co-currently.

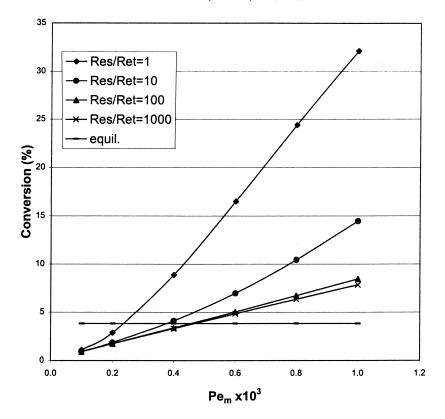


Fig. 1.  $H_2S$  conversion against  $Pe_m$  for  $Re^s/Re^t$  ratio of 1, 10, 100, and 1000 at the inlet temperature of 873 K.

Based on these assumptions, the steady-state mass and energy balances may be written as follows:

Tube side balances:

$$\frac{dP_{H_2S}^t}{dz} = -\left[\frac{(P_{tot}^t)^{1/2} P e_m d^t}{4U}\right] (-r_{H_2S}^t)$$
(3)

$$\frac{dP_{H_2}^t}{dz} = \left[\frac{(P_{tot}^t)^{1/2} P e_m d^t}{4U}\right] \left[ (-r_{H_2S}^t) - J_{H_2} \frac{S^t}{A^t} \right]$$
 (4)

$$\frac{\mathrm{d}z}{\mathrm{d}z} = \left[ \frac{4U}{U(P_{\text{tot}}^{t})^{1/2}\pi d^{t}C_{p_{\text{mix}}}^{t}} \right] \times \left[ (-\Delta H)(-r_{\text{H}_{2}S})A^{t} - S^{t}(T^{t} - T^{s}) \right] \times \left( J_{\text{H}_{2}}C_{p_{\text{H}_{2}}} + \frac{h}{2} \right)$$
(5)

Shell side balances:

$$\frac{dP_{H_2}^s}{dz} = \left[ \frac{P_{tot}^s P e_m R e^t d^t M_{mix} \mu_{mix}}{(P_{tot}^t)^{1/2} R e^s d^s M_{Ar} \mu_{Ar}} \right] J_{H_2}$$
 (6)

$$\frac{dT^{s}}{dz} = \left[ \frac{Pe_{m}Re^{t}M_{mix}\mu_{mix}}{Re^{s}M_{Ar}\mu_{Ar}U(P_{tot}^{t})^{1/2}\pi d^{s}C_{p_{mix}}^{s}} \right] \times \left[ S^{t}(T^{t} - T^{s}) \left[ J_{H_{2}}C_{pH_{2}} + \frac{h}{2} \right] + h^{f}S^{s}(T^{f} - T^{s}) \right]$$
(7)

with the boundary conditions at

$$z = 0, P_{H_2S}^t = P_{H_2S}^{in}, P_{H_2}^t = 0, P_{H_2}^s = 0,$$
  
 $T^t = T^{in}, T^s = T^{in}$  (8)

where

$$Re^{t} = \frac{4F_{\text{tot}}^{t}}{\pi M_{\text{mix}} d^{t} \mu_{\text{Ar}}}, \qquad Re^{s} = \frac{4F_{\text{tot}}^{s}}{\pi M_{\text{Ar}} d^{s} \mu_{\text{Ar}}}$$
(9)

$$Pe_{\rm m} = \frac{U(P_{\rm tot}^{\rm t})^{1/2} d^{\rm t} L \pi}{F_{\rm tot}^{\rm t}}$$
 (10)

Table 1 Heat of reaction and gas heat capacity parameters  $\Delta H_{298} = 85.2\,\mathrm{kJ/mol}$ 

,				
Component	ν	α	β	γ
H <sub>2</sub> S	-1	7.2	$3.6 \times 10^{-3}$	0
$S_2$	0.5	8.58	$3 \times 10^{-4}$	0
$H_2$	1	6.62	$8.1 \times 10^{-4}$	0

$$-r_{\rm H_2S} = k_{\rm H_2S} P_{\rm H_2S} - \frac{1}{K_{\rm eq}} (P_{\rm H_2})^{1/2}$$
 (11)

$$\ln K_{\rm eq} = \frac{10215.2}{T} - 2.44 \ln T \tag{12}$$

$$\Delta H = \Delta H_{298} + \int_{298}^{T} \Delta C_p \, \mathrm{d}T \tag{13}$$

$$\Delta C_p = \sum \nu_i C_{pi} \tag{14}$$

$$C_p = \alpha + \beta T^{t} + \gamma (T^{t})^2 \tag{15}$$

Values of  $\Delta H_{298}$ ,  $\nu$ ,  $\alpha$ ,  $\beta$ , and  $\gamma$  are presented in Table 1.

Table 2 Membrane reactor data and operating conditions

Parameter	Values	
Length of catalytic bed	0.6 m	
Diameter of reactor tube	$9.017 \times 10^{-3} \mathrm{m}$	
Diameter of reactor shell	$1.96 \times 10^{-2} \mathrm{m}$	
Thickness of platinum film	$5 \times 10^{-6} \mathrm{m}$	
Thickness of niobium membrane	$3 \times 10^{-3}  \text{m}$	
Pressure of reaction gas	101.325 kPa	
Pressure of sweep gas	50.663 kPa	
Furnace input temperature	1173 K	
$k_{ m H_2S}$	$7.11 \times 10^2 \mathrm{e}^{-92106/RT^t}$	
	$\mod(\mathrm{gcat})^{-1}\mathrm{s}^{-1}\mathrm{kPa}^{-1}$	

### 3. Results and discussion

The system of ordinary differential equations (Eqs. (3)–(8)) was solved using a fourth order Runge–Kutta method. It is, however, easily seen that the solution behavior will be a function of the fluid dynamics ( $Re^s$ ,  $Re^t$ ), membrane characteristics namely, cross-flow modified Peclet number,  $Pe_m$ , and inlet

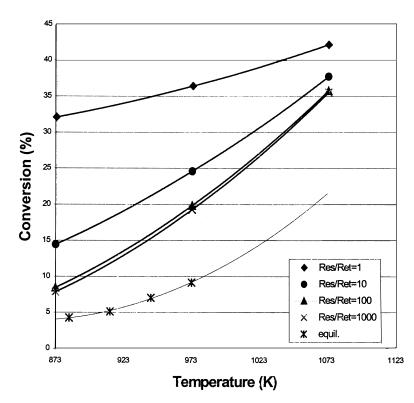


Fig. 2. Effect of temperature on  $H_2S$  conversion for  $Re^s/Re^t$  ratio of 1, 10, 100, and 1000 with  $Pe_m = 1 \times 10^{-3}$ .

temperature,  $T^{\text{in}}$  (both shell and tube sides). Consequently, the numerical results will be interpreted in terms of  $Re^{\text{s}}/Re^{\text{t}}$  ratio,  $Pe_{\text{m}}$  and  $T^{\text{in}}$ .

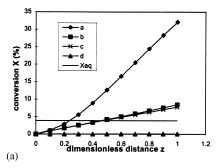
Table 2 provides a summary of the reactor specifications. Preliminary sensitivity analysis reveals that feasible solutions are only possible for  $10^{-5} \le Pe_{\rm m} \le 10^{-3}$  and  $Re^{\rm s}/Re^{\rm t} > 1$ .

Inlet temperature  $T^{\text{in}}$  was varied between 873 and 1073 K since catalytic rates are compounded by  $H_2S$  thermolysis at about 1043 K.

Fig. 1 shows that  $H_2S$  conversion increased monotonically with  $Pe_m$ . However, the effect was more pronounced at low  $Re^s/Re^t$  ratio with predicted reactor conversion of about eight times that at equilibrium (4%) at  $Pe_m = 10^{-3}$ . The increase in  $H_2S$  conversion with  $Pe_m$  is probably due to an increase in  $H_2$  flux across the membrane and thus reduced  $H_2$  partial pressure in the packed bed. In accordance with Le Chatelier's principle,  $H_2S$  decomposition in the packed bed would be shifted towards the right.

The relatively poor conversions recorded at  $Re^s/Re^t > 1$  is indicative of low transmembrane  $H_2$  flux at high sweep gas flow rates. A similar observation was made in the study of methane reforming in Pd membrane reactor [6]. As may be seen from Fig. 1, optimum  $H_2S$  conversion was obtained at  $Re^s/Re^t = 1$ . The effect of inlet temperature on  $H_2S$  conversion is illustrated in Fig. 2. It is apparent that conversion increased with temperature consistent with the endothermic nature of the reversible reaction. Interestingly, under all flow conditions investigated, the membrane reactor gave better conversions than thermodynamic equilibrium values.

Axial conversion profiles within the inner packed bed are shown in Fig. 3(i). The horizontal solid line corresponds to the equilibrium conversion at the inlet reactor condition. It is significant that conversion values are better almost anywhere in the reactor for  $Re^s/Re^t = 1$ . In particular conversion in excess of equilibrium were attained much earlier in the reactor than under the flow conditions in these plots. Fig. 3(ii) shows the influence of hydrodynamics and membrane properties on the  $H_2$  removal ratio, defined as the ratio of the  $H_2$  molar flow rate in the shell side to the  $H_2$  production rate in the tube side. Low  $Re^s/Re^t$  values favor the  $H_2$  removal ratio



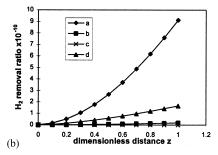
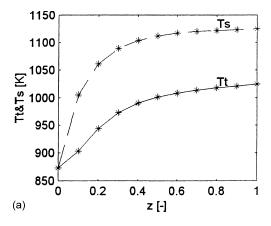
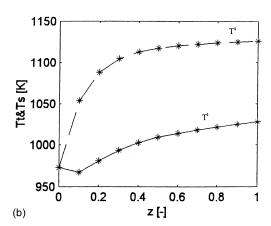


Fig. 3. (i) Axial conversion and (ii)  $H_2$  removal ratio profile. a:  $Pe_m=10^{-3},\ Re^s/Re^t=1$ ; b:  $Pe_m=10^{-3},\ Re^s/Re^t=100$ ; c:  $Pe_m=10^{-3},\ Re^s/Re^t=1000$ ; d:  $Pe_m=10^{-5},\ Re^s/Re^t=1$ .

at a given modified Peclet number,  $Pe_{\rm m}$ . However, when the latter is decreased by say two orders of magnitude even at  $Re^{\rm s}/Re^{\rm t}$ , the  $\rm H_2$  removal ratio substantially drops as may be seen by comparing curve a with d. Although not shown, the removal ratio does not change with inlet or reaction temperature.

Fig. 4 plots the temperature profile within the reactor. Inlet temperature appears to be a determinant of the axial temperature distribution at the lowest temperature studied (873 K). Temperature on both shell and tube sides rose monotonically from the inlet value before leveling off about half-way through the reactor to a plateau. However, the shell side temperature,  $T^s$  was always higher than the tube temperature,  $T^t$ , since the shell is directly in contact with the furnace wall maintained at 1173 K. There is, however a large temperature difference (100 K) between the quartz surface and the membrane wall. As the inlet temperature increased, the reaction side temperature,  $T^t$ , initially dropped before rising almost linearly to a





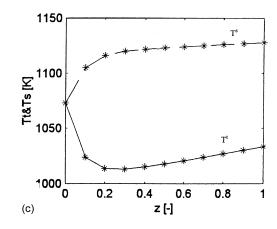


Fig. 4. (a) Temperature profile within the reactor for  $Re^s/Re^t=1$ ,  $Pe_m=1\times 10^{-3}$ , and inlet temperature at 873 K, (b) Temperature profile within the reactor  $Re^s/Re^t=1$ ,  $Pe_m=1\times 10^{-3}$ , and inlet temperature at 973 K, (c) Temperature profile within the reactor  $Re^s/Re^t=1$ ,  $Pe_m=1\times 10^{-3}$ , and inlet temperature at 1073 K.

higher exit temperature. The pattern is expected in an externally heated endothermic reactor operation and a similar behavior is also registered for  $T^{\rm in}=1073\,{\rm K}$ .  $T^{\rm s}$  profile in the shell side however was unchanged at all three inlet temperature levels probably because the temperature distribution is entirely governed by convective thermal transport since no reaction occurs within the annular space. Better conversions at low  $Re^{\rm s}/Re^{\rm t}$  ratio is evidence of better heat transfer to the membrane wall and hence the packed bed as a result of longer fluid residence time in the shell side.

# 4. Conclusion

This work has demonstrated that catalytic  $H_2S$  decomposition may offer higher than equilibrium conversion when carried out in an appropriate membrane reactor. Parametric studies based on steady-state non-isothermal model of the double pipe tubular reactor indicate that up to 8-fold increase in conversion (beyond thermodynamic limitation) may be obtained at low ratio of shell side Reynolds number to tube side Reynolds number. Conversion and hence  $H_2$  yield also improved with higher transmembrane modified Peclet number, although this value is bounded between  $10^{-5}$  and  $10^{-3}$ . Thus for a given membrane, material variation in  $Pe_m$  may be advanced by decreasing membrane thickness to improve overall  $H_2$  permeation coefficient.

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